

1 **MEASURING AMBIGUITY ATTITUDES FOR ALL**
2 **(NATURAL) EVENTS**

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12 Measurements of ambiguity attitudes have so far focused on artificial events,
13 where (subjective) beliefs can be derived from symmetry of events and then can be
14 controlled for. For natural events as relevant in applications, such a symmetry and
15 corresponding control are usually absent, precluding traditional measurement
16 methods. This paper introduces two indexes of ambiguity attitudes, one for aversion
17 and the other for insensitivity/perception, for which we can control for likelihood
18 beliefs even if those are unknown. Hence, we can now measure ambiguity attitudes
19 for natural events. Our indexes are valid under many ambiguity theories, do not
20 require expected utility for risk, and are easy to elicit in practice. We use our indexes
21 to investigate time pressure under ambiguity. People do not become more ambiguity
22 averse under time pressure, but become more insensitive (perceive more ambiguity).
23 These findings support the validity of our indexes.

24
25 JEL-CLASSIFICATION: D81, C91

26 KEYWORDS: ambiguity aversion; Ellsberg paradox; sources of uncertainty; time
27 pressure

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1

1. INTRODUCTION

2

Ambiguity (unknown probabilities) is central in many practical decisions (Keynes 1921; Knight 1921). Ellsberg's paradox (1961) showed that fundamentally new models are needed to handle ambiguity. Gilboa (1987), Gilboa and Schmeidler (1989), and Schmeidler (1989) introduced such new models, with many to follow.¹ Ambiguity theories are now widely applied (Easley and O'Hara 2009; Guidolin and Rinaldi 2013; Shaw 2016). However, measurements of ambiguity have been lagging behind, usually employing artificial laboratory events as in Ellsberg's paradox rather than the natural events that occur in practice.

10

To properly measure ambiguity aversion we need to control for likelihood beliefs in the events of interest, so as to calibrate the benchmark of ambiguity neutrality. But this control is difficult to implement for natural events. To illustrate this point, consider someone preferring to receive \$100 under the ambiguous event A of an increase in copper price of at least 0.01% next week rather than receiving \$100 under the risky event K of heads in a coin toss ($p = 0.5$) next week. This preference need not reflect ambiguity seeking. The person may be ambiguity neutral but assign a higher likelihood belief to A than to K . Without proper control of likelihoods, we therefore cannot know people's ambiguity attitudes. However, how to control for likelihoods using revealed preferences in a tractable manner has as yet been unknown for naturally occurring events.

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Controlling for likelihoods is easy for artificial events generated in the lab. Such events concern Ellsberg urns with color compositions kept secret from the subjects, or subjects only being informed about experimenter-specified probability intervals. Then likelihood beliefs can be derived from symmetry of colors or from symmetry about the midpoints of intervals. This explains why measurements of ambiguity have as yet focused on artificial events.

27

Several authors warned against the focus on artificial ambiguities, arguing for the importance of natural events (Camerer and Weber 1992 p. 361; Ellsberg 2011 p. 223;

28

¹ Theoretical surveys include Etner, Jeleva, and Tallon (2012), Gilboa and Marinacci (2016), Machina and Siniscalchi (2014), and Marinacci (2015).

1 Heath and Tversky 1991 p. 6; Trautmann and van de Kuilen 2015 p. 94). The
2 difficulty to identify (revealed preference based) likelihood beliefs of such events has
3 as yet been a problematic obstacle though. This paper introduces a simple method to
4 measure ambiguity attitudes for natural events. The solution to the aforementioned
5 problem is surprisingly easy: we control for likelihoods not by directly measuring
6 them but by making them drop from the equations irrespective of what they are. Our
7 method is tractable and easy to implement, as we demonstrate in an experiment.
8 Hence, it can for instance be easily used as an add-on in large-scale surveys and field
9 studies. Using natural events will increase external validity (Camerer and Weber
10 1992 p. 361).

11 Empirical studies, discussed later, have shown that ambiguity is a rich
12 phenomenon. Hence, two indexes are needed to capture ambiguity descriptively. The
13 first measures the well-known aversion to ambiguity and is often taken to be
14 normative. The second captures the degree of ambiguity, i.e., the perceived level of
15 ambiguity. Dimmock et al. (2015) therefore called their version of this index
16 perceived level of ambiguity. The higher this level is, the less the decision maker
17 discriminates between different degrees of likelihood, and the more these degrees are
18 treated alike, as one blur. The second index thus also captures insensitivity toward
19 likelihood changes, which is why we use the term a(mbiguity generated)-insensitivity.
20 Empirical studies have found that (uncorrected) ambiguity aversion is likelihood
21 dependent, even with prevailing ambiguity seeking, rather than aversion, for unlikely
22 gain-events (Trautmann and van de Kuilen 2015). That is, ambiguity aversion even
23 predicts in the wrong direction for such events. This illustrates the desirability to use
24 the second index to correct for this likelihood dependence.

25 To summarize, relative to their predecessors, our indexes: (a) correct for
26 subjective likelihoods also if unknown and, hence, which is our main novelty: (b) can
27 be used for all events, both artificial and natural; (c) correct for likelihood dependence
28 of ambiguity aversion. Further, as discussed later, our indexes (d) are directly
29 observable; (e) are valid under many ambiguity theories, unifying preceding indexes;
30 in particular, they (f) retain validity if expected utility for risk is violated. Our paper
31 also shows that the ambiguity aversion index can better be related to matching
32 probabilities than to nonadditive weighting functions as done before (Dow and
33 Werlang 1992); see §5.

1 Our indexes will be defined for three-fold partitions. The follow-up paper
 2 Baillon, Li, and Wakker (2017), a theoretical counterpart to this paper, provides a
 3 theoretical foundation of our indexes, and generalizations to general partitions. It
 4 shows that our indexes are valid for a large number of ambiguity theories, being all
 5 that evaluate prospects $\gamma_E 0$ (yielding one nonzero outcome, γ , under event E , and 0
 6 otherwise) by a product $W(E)U(\gamma)$.² This implies, in particular, that we assume only
 7 one utility function U , for risk and all sources of uncertainty. Here we deviate from
 8 utility-based models of ambiguity, such as the popular smooth model (Klibanoff,
 9 Marinacci, and Mukerji 2005).³ Using tools of Izhakian and Brenner (2011), Baillon,
 10 Li, and Wakker (2017) shows that our indexes are nevertheless also useful under the
 11 smooth model.⁴ Our indexes thus unify and generalize many existing indexes (point
 12 (e) above). Baillon, Li, and Wakker (2017) also shows that our two indexes capture
 13 orthogonal, i.e., completely distinct, components of the data. This mathematical
 14 separation homeomorphically⁵ supports the psychological interpretation of the
 15 indexes as distinct components (motivational versus cognitive) and the empirical
 16 desirability to consider both. This paper will support these points empirically.

² As yet, indexes proposed in the literature concerned only one ambiguity theory. In the same way as no risk aversion index can be valid for all risk theories, our ambiguity indexes cannot be valid for all ambiguity theories. Yet, they are for many. Such theories include biseparable utility (Ghirardato and Marinacci 2002), which in turn includes Choquet expected utility (Schmeidler 1989), prospect theory for gains (Tversky and Kahneman 1992), and the α -maxmin model (Ghirardato, Maccheroni, and Marinacci 2004; Jaffray 1994; our Eq. 5.1 shows how to derive α from our indexes). Some nonbiseparable theories that are included: separate-outcome weighting theories ($x_E y \rightarrow W(E)U(x) + W(E^c)U(y)$; Einhorn and Hogarth 1985), Chateauneuf and Faro's (2009) confidence representation if the worst outcome is 0, and Lehrer and Teper's (2015) event-separable representation.

³ Other utility-based theories not included are: Chew et al. (2008), Dobbs (1991), Nau (2006), and Neilson (2010). Further theories not included are: Chateauneuf and Faro (2009) in general, Gul and Pesendorfer (2014), Izhakian (2017), Olszewski (2007), and Siniscalchi (2009).

⁴ That is, our indexes provide local ambiguity premiums in probability units that are analogous to Pratt's (1964 Eq. 5) local risk premium, which was in money units. This result also holds for a subclass of Maccheroni, Marinacci, and Rustichini's (2006) variational model.

⁵ That is, not only observable results but also underlying processes in the model agree with real processes.

1 Because a-insensitivity has been less known than ambiguity aversion, and
 2 different interpretations are possible for our insensitivity index, we test how our two
 3 indexes react to cognitive manipulations. For this purpose, we use time pressure (TP).
 4 TP has received special attention in the psychological literature because it provides a
 5 good context for manipulating cognitive limitations, in addition to its practical
 6 relevance (Ariely and Zakay 2001; Essl and Jaussi 2017). De Paola and Gioia (2015)
 7 and Spiliopoulos and Ortmann (2017) argued for the usefulness of TP and, relatedly,
 8 response time, as a tool in experimental economics and for its relevance in economic
 9 applications. Despite the many studies of TP under risk (known probabilities;
 10 references are in §4.4) there have not yet been studies of TP under ambiguity.
 11 Providing the first such study is an additional contribution of our paper. Our findings
 12 corroborate the interpretation of the indexes, supporting the validity of our method. In
 13 particular, they illustrate the usefulness of our second index.

14 The outline of this paper is as follows. Section 2 gives formal definitions of our
 15 ambiguity indexes and informal arguments for their plausibility. We present the
 16 indexes without assuming any decision theory so that empirically oriented readers can
 17 readily use them with no need to study such a theory. This also shows that the
 18 indexes have intuitive appeal without requiring a commitment to one of the many
 19 ambiguity theories popular today. Sections 3-4 demonstrate the validity of our
 20 indexes empirically, and Sections 5-6 discuss and conclude. Experimental details are
 21 in the appendix, with further details in an Online Appendix.

22

23 2. MEASURING AMBIGUITY ATTITUDES WITHOUT 24 MEASURING SUBJECTIVE LIKELIHOODS: DEFINITIONS 25 OF OUR INDEXES

26 We focus on gain outcomes throughout this paper. Formally speaking, ambiguity
 27 does not concern just a single event E , but a partition, such as $\{E, E^c\}$, or, more
 28 generally, a source of uncertainty. We assume a minimal degree of richness of the
 29 sources of uncertainty considered: there should be three mutually exclusive and
 30 exhaustive nonnull events E_1, E_2 , and E_3 . In many situations where we start from a
 31 partition with two events we can extend it by properly partitioning one of those two

1 events. For example, in the two-color Ellsberg urn we can involve other features of
 2 the ball to be drawn, such as shades of colors or numbers on the balls. In our
 3 experiment, the events refer to the AEX stock index. For instance, in Part 1 of the
 4 experiment, $E_1 = (-\infty, -0.2)$, $E_2 = [-0.2, 0.2]$, and $E_3 = (0.2, \infty)$, where intervals
 5 describe percentage increases of the AEX index during the experiment. Thus, they
 6 concern natural events with uncertainty that really occurred and that was of practical
 7 relevance to financial traders. E_{ij} denotes the union $E_i \cup E_j$, where $i \neq j$ is implicit.
 8 We call every E_i a *single event* and every E_{ij} a *composite event*.

9 Dimmock, Kouwenberg, and Wakker (2016, Theorem 3.1) showed that matching
 10 probabilities are convenient for measuring ambiguity attitudes. Early applications
 11 include Kahn and Sarin (1988) and Viscusi and Magat (1992). They are a central
 12 theoretical tool in Izhakian's (2017) ambiguity theory. Karni (2009) discussed their
 13 empirical elicitation. Matching probabilities entirely capture ambiguity attitudes, free
 14 from any complications regarding risk attitudes, because those drop from the
 15 equations and need not be measured. In particular, our measurements are not affected
 16 by the large heterogeneity of risk attitudes (Bruhin, Fehr-Duda, and Epper 2010). We
 17 will, therefore, use matching probabilities. An admitted drawback of matching
 18 probabilities is that their assessment is cognitively harder than, for instance, of
 19 certainty equivalents (Bleichrodt, Pinto, and Wakker 2001 p. 1505; Callen et al. 2013
 20 p. 136; Halter and Beringer 1960 p. 124)—a pro is that they can be measured for all
 21 kinds of outcomes, also if nonquantitative. For any fixed prize (€20 in our
 22 experiment), we define the *matching probability* m of event E through the following
 23 indifference:

24 Receiving €20 under event E is equivalent to receiving €20 with probability m . (2.1)

25 In both cases it is understood that the complementary payoff is nil. Under ambiguity
 26 neutrality, the matching probability of an event, say $m(E_1)$, and its complement,
 27 $m(E_{23})$, will add to 1, but under ambiguity aversion the sum will fall below 1. Its
 28 difference with 1 can then be taken as the degree of aversion. We will take the
 29 average of this difference over the three events. We write $m_i = m(E_i)$, $m_{ij} =$
 30 $m(E_{ij})$, $\bar{m}_s = (m_1 + m_2 + m_3)/3$ for the average single-event matching probability,
 31 $\bar{m}_c = (m_{12} + m_{13} + m_{23})/3$ for the average composite-event matching probability,
 32 and define:

1

2 DEFINITION 2.1. The *ambiguity aversion index* is

3
$$b = 1 - \overline{m}_c - \overline{m}_s. \tag{2.2}$$

4

5 Note that no statistical claims or randomness assumptions are made at this stage
6 in this definition. We use a deterministic calculation here, recoding direct
7 observations. Under ambiguity neutrality⁶, $m_i = P(E_i)$ and $m_{ij} = P(E_i) + P(E_j)$ for
8 some additive subjective probability measure P . Then $\overline{m}_s = 1/3$ and $\overline{m}_c = 2/3$,
9 implying $b = 0$. We have thus calibrated ambiguity neutrality, providing control for
10 subjective likelihoods even though we do not know them. This happens because the
11 subjective likelihoods drop from the equations irrespective of what they are. This
12 observation is key to our method. Maximal ambiguity aversion occurs for $b = 1$.
13 Then the matching probabilities of all events are 0. Ambiguity aversion is minimal
14 for $b = -1$, when matching probabilities for all events are 1.

15 The ambiguity aversion index can also be defined if we only consider a two-event
16 partition. We can focus on only one event E_i and its complement E_i^c , and substitute
17 $m(E_i)$ for \overline{m}_s and $m(E_i^c)$ for \overline{m}_c in Eq. 2.2, maintaining the control for likelihood.
18 This would reduce the measurement effort—at the cost of reliability. For the
19 insensitivity index defined next we, to the contrary, essentially need three events.

20 Theoretically, the second index captures the extent to which matching
21 probabilities and event weights regress towards fifty-fifty, with low likelihoods
22 overvalued and high likelihoods undervalued. This leads to reduced differences
23 $\overline{m}_c - \overline{m}_s$. In the most extreme case of complete ambiguity and, correspondingly,
24 complete insensitivity (Cohen and Jaffray 1980), no distinction at all is made between
25 different levels of likelihood (e.g. all events are taken as fifty-fifty), resulting in
26 $\overline{m}_c - \overline{m}_s = 0$. These observations suggest that the second index can be interpreted as a
27 cognitive component (Budescu et al. 2014 p. 3; Dimmock et al. 2015; Dimmock,

⁶ When objective probabilities are assumed present in the domain considered, as is our case, then ambiguity neutrality is equivalent to probabilistic sophistication (Dean and Ortleva 2017 p. 393 footnote 1). If no objective probabilities are present, such as when only considering the unknown Ellsberg two-color urn, then probabilistic sophistication is strictly more general—but then matching probabilities, and our indexes, cannot even be defined.

1 Kouwenberg, and Wakker 2016; Einhorn and Hogarth 1985; Gayer 2010), an
 2 interpretation well supported by our results. For this index, the following rescaling of
 3 $\overline{m}_c - \overline{m}_s$ is convenient.

4

5 DEFINITION 2.2. The *ambiguity-generated insensitivity (a-insensitivity) index*⁷ is

$$6 \quad a = 3 \times \left(\frac{1}{3} - (\overline{m}_c - \overline{m}_s) \right) . \quad (2.3)$$

7 Under ambiguity neutrality, with perfect discrimination between single and composite
 8 events, or under absence of ambiguity, $\overline{m}_c = 2/3$ and $\overline{m}_s = 1/3$, and their difference
 9 is $1/3$. Index a measures how much the actual difference falls short of $1/3$. We
 10 multiplied by 3 to obtain a convenient normalization with a maximal value 1
 11 (maximal insensitivity, with $\overline{m}_c = \overline{m}_s$).

12 Ambiguity neutrality gives $a = 0$. We have again calibrated ambiguity neutrality
 13 here, controlling for subjective likelihoods by letting them drop from the equations.
 14 Empirically, we usually find prevailing insensitivity, $a > 0$, but there are subjects
 15 with $a < 0$. Hence it is desirable for descriptive purposes to allow $a < 0$, which we
 16 do. The α -maxmin model, however, does not allow $a < 0$ (Baillon, Li, and Wakker
 17 2017), which is no problem for normative applications that take $a < 0$ to be irrational.

18 Our two indexes are orthogonal (Baillon, Li, and Wakker 2017). If one is 0,
 19 suggesting ambiguity neutrality, the other may still deviate from 0, showing
 20 ambiguity attitude. In particular, contrary to what has sometimes been suggested in
 21 the literature, if there is no aversion to ambiguity, then ambiguity may still play an
 22 important role through insensitivity.⁸

23 Dimmock et al. (2015) referred to their version of the second index as perceived
 24 level of ambiguity. Dimmock et al.'s term, and the multiple priors model underlying
 25 it, may serve best for applications that, unlike this paper, have normative aims. Their
 26 assumption of expected utility for risk, and their restriction $a \geq 0$, are problematic for
 27 descriptive applications though. For risk, insensitivity (i.e., inverse-S probability
 28 weighting) has been commonly found (Fehr-Duda and Epper 2012; Wakker 2010

⁷ Under multiple prior theories, this index can be called “perceived level of ambiguity.”

⁸ For instance, in Schmeidler (1989), with W denoting the weighting function, $W(E) + W(E^c) = 1$ may hold for all events E , while there may still be strong insensitivity.

1 §9.5). Our second index naturally extends this insensitivity found under risk to
2 ambiguity, where empirical studies have found that it is usually amplified (Trautmann
3 and van de Kuilen 2015; Wakker 2010 p. 292). Hence, we use the term ambiguity-
4 generated insensitivity (a-insensitivity) to refer to it. Insensitivity was central in the
5 early Einhorn and Hogarth (1985). Gonzalez and Wu (1999) gave an illuminating
6 discussion of its psychological interpretations, for risk. The textbook Wakker (2010,
7 §10.4.2 and §11.8) presents the concept for ambiguity.

8

9

10 3. EXPERIMENT: METHOD

11 This section presents the experiment. Appendix A gives further details. We
12 investigate the effect of time pressure (TP) on ambiguity. The ambiguity concerns the
13 performance of the AEX (Amsterdam stock exchange) index. Using our method, we
14 can study TP for natural events.

15

16 *Hypotheses*

17 It is natural to expect that TP will reduce cognitive understanding and, hence, increase
18 the insensitivity index. This is the hypothesis we test. We had no prior prediction
19 about the impact of TP on ambiguity aversion. Ambiguity aversion reflects how
20 much *more* there is dislike for uncertainty than for risk. We saw no reason for this
21 difference to become bigger or smaller.

22

23 *Subjects*

24 N = 104 subjects participated (56 male, median age 20). They were all students from
25 Erasmus University Rotterdam, recruited from a pool of volunteers. They were
26 randomly allocated to the control and the TP treatment.

27 The experiment consisted of two parts, Parts 1 and 2 (Table 1), consisting of eight
28 questions each. They were preceded by a training part (Part 0) of eight questions, to
29 familiarize subjects with the stimuli. All subjects faced the same questions, except that
30 subjects in the TP treatment had to make their choices in Part 1 under time pressure.

1 There were 42 subjects in the control treatment and 62 in the TP treatment. The TP
2 sample had more subjects because we expected more variance there.

3

4 TABLE 1: Organization of the experiment

Within subject Between subject	<i>Part 1</i>	<i>Part 2</i>
Control treatment	No time pressure	No time pressure
Time pressure treatment	Time pressure	No time pressure

5 Stimuli: Within- and between-subject treatments

6

7 *Stimuli: Choice lists*

8 In each question, subjects were asked to choose between two options.

9

10 OPTION 1: You win €20 if the AEX index increases/decreases by ... between the
11 beginning and the end of the experiment (which lasted 25 minutes on average), and
12 nothing otherwise.

13 OPTION 2: You win €20 with p% probability and nothing otherwise.

14

15 We used choice lists to infer the probability p in Option 2 that leads to
16 indifference between the two options; see the Appendix for details. This p is the
17 matching probability of the AEX event. For the TP treatment, a 25-second time limit
18 was set for each choice in Part 1.

19

20 *Stimuli: Uncertain events*

21 In each part we consider a triple of mutually exclusive and exhaustive single events
22 and their compositions; see Table 2.

23

24 TABLE 2: Single AEX-change events for different parts (unit is percentage)⁹

	Event E ₁	Event E ₂	Event E ₃
Part 1	$(-\infty, -0.2)$	$[-0.2, 0.2]$	$(0.2, \infty)$
Part 2	$(-\infty, -0.1)$	$[-0.1, 0.3]$	$(0.3, \infty)$

⁹ In the training Part 0, the events were $(-\infty, -0.4)$, $[-0.4, 0.1]$, and $(0.1, \infty)$.

1

2 We chose the partition in Part 2 somewhat differently to make subjects choose afresh
3 rather than erroneously speculate on relations between the questions. For each part,
4 we measured matching probabilities of all six single and composite events, of which
5 two were repeated to test consistency. The order of the eight questions was
6 randomized for each subject within each part.

7

8 *Stimuli: Further questions*

9 At the end of the experiment, subjects were asked to report their age, gender, and
10 nationality.

11

12 *Incentives*

13 We used the random incentive system. All subjects received a show-up fee of €5 and
14 one of their choices was randomly selected to be played for real; see the Appendix for
15 details. This implies, as usual, that the truth of the events must be observable for
16 payment, so that uncertainties in a far future, for instance, cannot be incentivized this
17 way.

18

19 *Analysis*

20 We computed ambiguity aversion and a-insensitivity indexes as explained in §2. Five
21 subjects in the TP treatment did not submit one of their matching probabilities on time
22 and were therefore excluded from the analysis, leaving us with 99 subjects.

23 We ran OLS regressions to study the impact of TP on a-insensitivity and
24 ambiguity aversion. Because we obtain two values of each index per subject (one for
25 each part), we clustered standard errors at the individual level. Furthermore, because
26 the residuals of the regression on a were correlated with the residuals of the
27 regression on b , we used Seemingly Unrelated Regressions. In the baseline model
28 (Model 1 in the result tables), we take Part 1 in the control treatment as the reference
29 group and consider three dummy variables: part 2*control, part 1*TP and part 2*TP,
30 where each variable takes value 1 if the observation is from the specific part in the
31 specific treatment. We then add control variables (age, gender, and nationality in
32 Model 2) to assess the robustness of the results.

33

34 We analyze responses time to verify that subjects answered faster in the TP
treatment. To do so, we run OLS regressions for the response time with clustered

1 standard errors, as for the indexes. For some events we elicited the matching
 2 probabilities twice to test for consistency, since TP can be expected to decrease
 3 consistency. For each treatment and each part, we compare the first and second
 4 elicitation of these matching probabilities using t-tests with the Bonferroni correction
 5 for multiple comparisons. In the rest of the analysis, we only use the first matching
 6 probability elicited for each event.

7 By set-monotonicity, the matching probability of a composite event should
 8 exceed the matching probability of either one of its two constituents. Thus, we can
 9 test set-monotonicity six times in each part. *Weak monotonicity* is defined by
 10 $\overline{m_c} \geq \overline{m_s}$. It ensures $a \leq 1$. Violations of weak monotonicity entail very erratic
 11 answers. We nevertheless kept all answers in the analysis. Excluding the indexes
 12 when weak monotonicity is violated does not affect our conclusions (see the full
 13 results in the Online Appendix) unless we report otherwise. We will run non-
 14 parametric analysis (Wilcoxon tests and Mann-Whitney U tests) to test whether time
 15 pressure had an impact on the number of set-monotonicity and weak monotonicity
 16 violations.

17

18

4. EXPERIMENT: RESULTS

19 Table 3 gives descriptive results for the ambiguity indexes.

20

21 TABLE 3: Descriptive statistics

		a (part 1)	a (part 2)	b (part 1)	b (part 2)
Control	<i>mean</i>	.15	.17	-.07	-.11
	<i>standard deviation</i>	.44	.41	.21	.24
	<i>standard error</i>	.07	.06	.03	.04
	<i>median</i>	.07	.20	-.08	-.10
	<i>N</i>	42	42	42	42
TP	<i>mean</i>	.34	.17	-.09	-.06
	<i>standard deviation</i>	.44	.45	.24	.24
	<i>standard error</i>	.06	.06	.03	.03
	<i>median</i>	.35	.11	-.08	-.11
	<i>N</i>	57	57	57	57

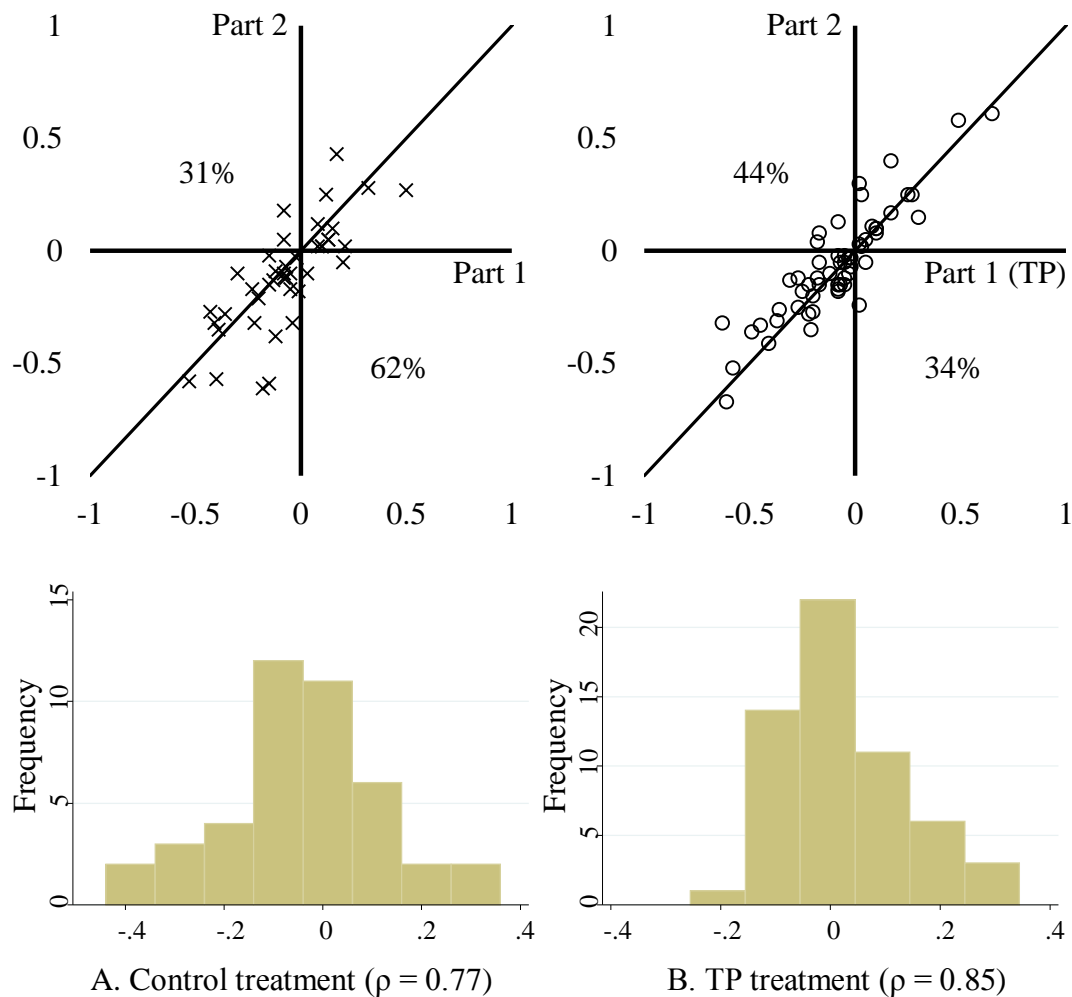
22

1 In what follows, we discuss only differences that are significant, with the
2 significance level indicated in the corresponding tables.

4 4.1. Ambiguity Aversion Index b

5 To first illustrate the general nature of our data, Figure 1 presents all b indexes of
6 Part 2 as a function of the b indexes of Part 1. Spearman correlations are high ($\rho =$
7 0.77 for the control treatment and $\rho = 0.85$ for the TP treatment) and most dots are in
8 the lower left quadrant or in the upper right quadrant. It shows that subjects are
9 consistently ambiguity averse or consistently ambiguity seeking across parts.

10
11 FIGURE 1: ambiguity aversion indexes b



Percentages of observations above and below the diagonal have been indicated in the figures. Spearman correlations ρ are in the panel titles. The histograms represent the distribution of the index difference between Part 1 and Part 2.

1 Table 4 displays the results of the panel regressions for the b indexes. In Part 1,
 2 the control subjects are slightly ambiguity seeking (-0.07), with the dots in panel A
 3 slightly to the left. Regarding our main research question: the null hypothesis that TP has
 4 no effect cannot be rejected. The index b in TP does not differ significantly from that in
 5 the control in Part 1, with dots in panel B not more or less to the left than in panel A. The
 6 only effect we find is a learning effect for the control treatment, where Part 2 is a
 7 repetition of Part 1.¹⁰ Here ambiguity aversion is lower in Part 2 than in Part 1. There is
 8 no learning effect for the TP treatment ($p = 0.14$). This may be because TP in Part 1
 9 prevented the subjects to familiarize further with the task.

10 All aforementioned effects, and their levels of significance, are unaffected when
 11 we control for age, gender, and nationality (Dutch / non-Dutch) in Model 2. To test if
 12 ambiguity aversion, while not systematically bigger or smaller under TP, would
 13 become more or less extreme, we test absolute values of b , but find no evidence for
 14 such effects (see Online Appendix).

15
 16 TABLE 4: ambiguity aversion indexes b

	Model 1	Model 2
intercept	-0.07^* (0.03)	0.02 (0.06)
part 1 * TP treatment	-0.02 (0.05)	-0.03 (0.04)
part 2 * control treatment	-0.04^\dagger (0.02)	-0.04^\dagger (0.02)
part 2 * TP treatment	0.00 (0.05)	-0.01 (0.04)
male		-0.08^\dagger (0.04)
Dutch		-0.07 (0.05)
age – 20		0.02 (0.02)
Chi2	6.42 [†]	18.48 ^{***}
N	198	198

[†] $p < 0.1$, * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$. Point estimates are followed by standard errors between brackets. The impact of TP is in bold. The variable age has been recoded as age – 20 so that the intercept corresponds to the b index of a 20 year-old subject (median age).

17

¹⁰ The learning effect is marginally significant and not significant anymore if we exclude the subjects violating weak monotonicity (see Table OB.1 in Online Appendix). So as to avoid learning effects for the part with TP, we had it precede the part without TP.

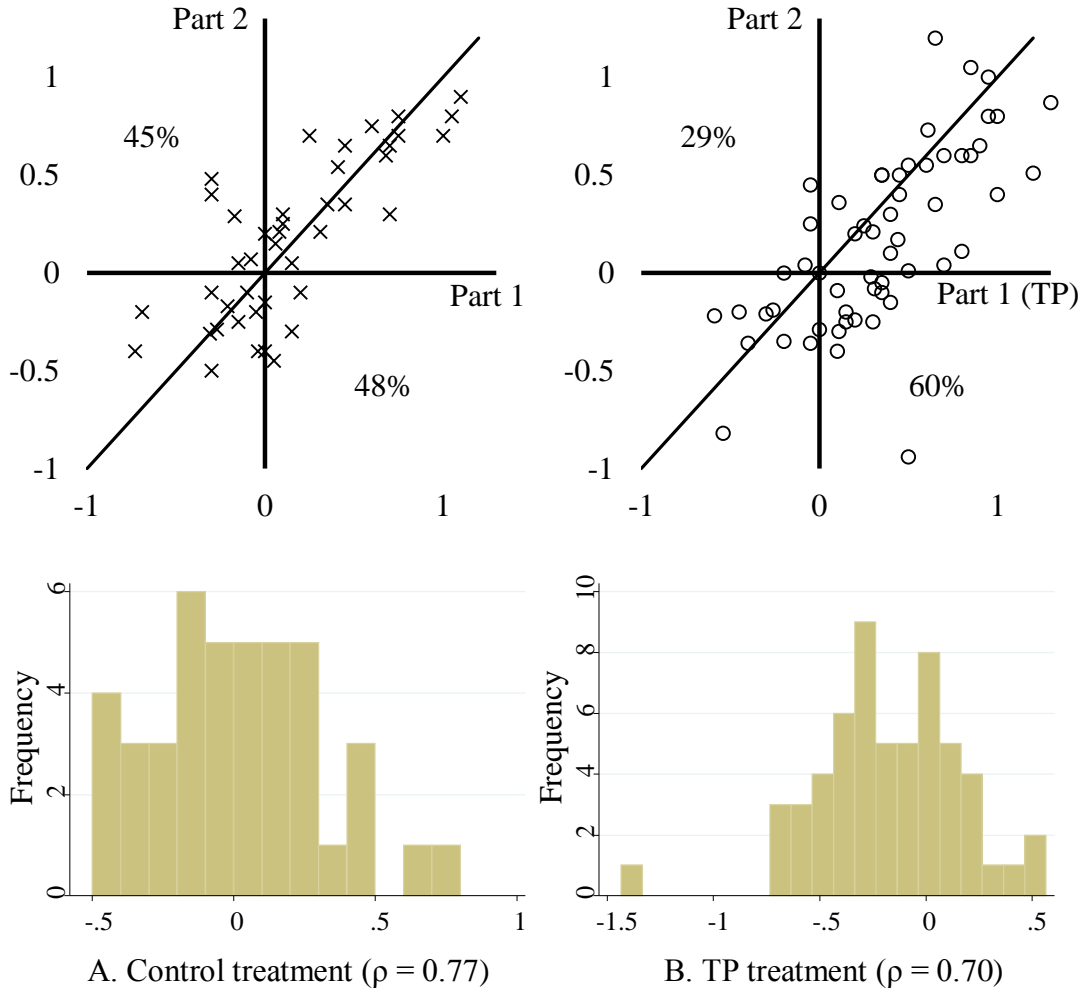
4.2. A-Insensitivity Index a

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2

3 FIGURE 2: a-insensitivity indexes a

4



5

6

7 Percentages of observations above and below the diagonal have been indicated in the
 8 figures. Spearman correlations ρ are in the panel titles. The histograms represents
 9 the distribution of the index difference between Part 1 and Part 2.

10

11 Figure 2 depicts all individual a indexes of Part 2 as a function of the a indexes
 12 of Part 1. Spearman correlations are again high ($\rho = 0.73$ for the control treatment
 13 and $\rho = 0.74$ for TP). Table 5 displays the results of the panel regressions for the a
 14 index. The insensitivity index is between 0.15 and 0.17 for Parts 1 and 2 of the
 15 control treatment (no learning effect and points equally split above and below the
 16 diagonal in panel A), and also for Part 2 of the TP treatment. However, there is much
 17 more a-insensitivity for the TP questions (Part 1 of TP treatment), with $a = 0.34$ and

1 with two-thirds of the dots in panel B to the right of the diagonal. These findings are
 2 robust to the addition of control variables (Model 2). Thus, we find a TP effect but no
 3 evidence for a learning effect.

4

5 TABLE 5: a-insensitivity indexes a

6

	Model 1	Model 2
intercept	0.15 [*] (0.07)	0.20 [†] (0.12)
part 1 * TP treatment	0.19[*] (0.09)	0.18[*] (0.09)
part 2 * control treatment	0.02 (0.04)	0.02 (0.04)
part 2 * TP treatment	0.02 (0.09)	0.01 (0.09)
male		-0.05 (0.08)
Dutch		-0.06 (0.09)
age - 20		0.02 (0.02)
Chi2	16.19 ^{***}	18.36 ^{***}
N	198	198

[†] $p < 0.1$, * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$. Point estimates are followed by standard errors between brackets. The impact of TP is in bold. The variable age has been recoded as age - 20 so that the intercept corresponds to the a index of a 20 year-old subject (median age).

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4.3. Response Time, Consistency, and Monotonicity

10 The average response time in the training part is more than 25 seconds, but it gets
 11 much lower in Part 1 and then again in Part 2 for both the control and the TP
 12 treatment. Understandably, subjects needed to familiarize with the task. In Table 6,
 13 the benchmark model (Model 1) shows that the average response time of the control
 14 subjects in Part 1 is about 17s per matching probability. It is about 4s longer than for
 15 subjects under TP, even though the TP-treatment subjects could spend up to 25s to
 16 answer. In Part 2, the control subjects answered faster than in Part 1.

1 TABLE 6: Response time

2

	Model 1	Model 2
intercept	16.63 ^{***} (1.33)	16.66 ^{***} (1.44)
part 1 * TP treatment	-4.13^{**} (1.40)	-4.44^{**} (1.44)
part 2 * control treatment	-2.33 [*] (1.14)	-2.33 [*] (1.14)
part 2 * TP treatment	-1.77 (1.74)	-2.08 (1.79)
male		-1.45 (1.21)
Dutch		0.99 (1.19)
age – 20		0.48 (0.32)
R ²	0.02 ^{**}	0.03 ^{**}
N	1584	1584

[†] p < 0.1, * p < 0.05, ** p < 0.01, *** p < 0.001. Point estimates are followed by standard errors between brackets. The impact of TP is in bold. The variable age has been recoded as age – 20 so that the intercept corresponds to the response time of a 20 year-old subject (median age). The stars reported next to R² refers to F-tests of overall significance.

3

4 We next analyze the consistency of the matching probabilities by comparing
5 repeated elicitations of matching probabilities for some events. Pairwise comparisons
6 for each pair of matching probabilities with the Bonferroni correction indicate one
7 difference, in one of the two tests in Part 1 for the TP treatment: the second matching
8 probability m_{13} is higher than the first one (mean difference = 0.04; p = 0.01). The
9 other differences are not significant.

10 A similar pattern is found in the set-monotonicity tests. Out of 6 monotonicity
11 tests, the average number of violations is 0.58 in Part 1 for the TP treatment, while it
12 is only 0.30 in Part 2 for the same treatment and 0.36 and 0.24 in Parts 1 and 2,
13 respectively, for the control treatment. The difference between Parts 1 and 2 in the TP
14 treatment is significant (within-subject Wilcoxon signed-ranks test; $Z = -2.61$, p =
15 0.01) and the difference between the TP and the control treatment in Part 1 is
16 marginally significant (between-subject Mann-Whitney U test; $Z = -1.71$, p = 0.09).
17 The percentage of weak monotonicity violations is 5% and 4% in Parts 1 and 2 for the
18 TP treatment, and 5% and 0% in Parts 1 and 2 for the control treatment. None of the
19 differences is significant.

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4.4. *Summary and Discussion of the Experiment*

We summarize the experimental results. TP indeed increases insensitivity (index *a*), as predicted. That TP harms cognitive understanding is further confirmed by increased violations of consistency and set-monotonicity. These findings confirm Ariely and Zakay's (2001) observation that TP aggravates biases and irrationalities. TP does not increase or decrease ambiguity aversion (index *b*).

Somewhat similar to our results, Young et al. (2012) found that TP increases insensitivity under risk. The effects of TP on risk aversion are not clear and can go in either direction (Young et al. 2012; Kircher et al. 2017; Kocher, Pahlke, and Trautmann 2013), consistent with our absence of effect on ambiguity aversion. Kocher, Pahlke, and Trautmann (2013) also found increased insensitivity toward outcomes under TP for risk. Tinghög et al. (2013) confirmed a more pronounced four-fold pattern of risk, again in agreement with increased insensitivity. Our second index will therefore be useful for future studies, nudging techniques, and policy recommendations regarding TP. Whereas the (ir)rationality of ambiguity aversion has been widely debated, insensitivity clearly reflects cognitive limitation and irrationality. Thus, the increased demand of full insurance and decreased demand for precautionary and partial insurance found by Bajtelsmit, Coats, and Thistle (2015) perfectly fits with insensitivity, as does the decreased quality of decisions in Conte, Scarsini, and Sürücü (2016), De Paola and Gioia (2015), and Kirchler et al. (2017). Our study therefore supports the desirability to avoid TP for important decisions.

The absence of ambiguity aversion in our results is not surprising in view of recent studies with similar findings, especially because we used natural events rather than Ellsberg urns (Binmore, Stewart, and Voorhoeve 2012; Charness, Karni, and Levin 2013; Kocher, Lahno, and Trautmann 2017; Trautmann and van de Kuilen 2015). An additional experimental advantage of using natural events—that suspicion about experimenter-manipulated information is avoided—may have contributed to the absence of ambiguity aversion in our study. Such suspicion is further excluded because subjects always bet both on events and on their complements. In fact, suspicion may have worked against the risky events, because the natural events were even more verifiable than the risky events. Finally, the increase in preference (index

1 *b*) in Part 2 of the control treatment is in agreement with the familiarity bias (Chew,
2 Ebstein, and Zhong 2012; Fox and Levav 2000; Kilka and Weber 2001).

3 The events in our experiments were natural in the sense of not involving any
4 artificial concealing of information. We did not consider them in an actually
5 occurring natural decision situation or in a field setting, and the decision situations
6 considered were experimental. However, we used uncertainty that actually occurred
7 and that was relevant to financial traders.

8

9 5. GENERAL DISCUSSION

10 Indexes are simplified summaries of complex realities. Our indexes cannot be
11 expected to perfectly capture ambiguity attitudes, in the same way as the well-known
12 index of relative risk aversion (IRR) cannot be expected to perfectly capture risk
13 attitudes for every decision and every theory. The IRR does perfectly describe risk
14 attitudes under expected utility with CRRA utility. For other utility functions, it will
15 only work well on restricted domains of outcomes (Wakker 2008). Similarly, our
16 indexes do perfectly describe ambiguity attitudes under Chateauneuf, Eichberger, and
17 Grant's (2007) neo-additive event weighting for several ambiguity theories (Baillon,
18 Li, and Wakker 2017). In general, they will work well if none of the events in the
19 partition is very likely or unlikely. Violations of event additivity and neo-additive
20 weighting occur primarily for extreme events where no theory describes the many
21 irregularities very well.¹¹

22 There have as yet only been a few studies measuring ambiguity attitudes for
23 natural events. Many did not control for risk attitudes and therefore could not
24 completely identify ambiguity attitudes (Baillon et al. 2017; Fox, Rogers, and Tversky
25 1996; Fox and Tversky 1998; Kilka and Weber 2001). Abdellaoui et al. (2011)
26 measured indexes similar to ours but had to use complex measurements and data
27 fittings, requiring measurements of subjective probabilities, utilities, and event
28 weights. As regards the treatment of unknown beliefs, Brenner and Izhakian (2015)

¹¹ Thus, for risk, Kahneman and Tversky (1979 pp. 282-283) explicitly refrained from specifying any shape of probability weighting for extreme probabilities.

1 and Gallant, Jahan-Parvar, and Liu (2015) are close to us. They do not assume beliefs
 2 given beforehand, but, like Abdellaoui et al. (2011), derive them from preferences.
 3 We do not need such derivations. Brenner and Izhakian (2015) and Gallant, Jahan-
 4 Parvar, and Liu (2015) deviate from our approach in assuming second-order
 5 probabilities to capture ambiguity. They make parametric assumptions about the first-
 6 and second-order probabilities (assuming normal distributions), including expected
 7 utility for risk with constant relative risk aversion, and then fit the remaining
 8 parameters to the data for a representative agent. Maccheroni, Marinacci, and
 9 Ruffino's (2013) theoretical analysis follows a similar approach. A difficulty in
 10 parametric fittings often concerns what can be taken as ambiguity neutrality.

11 Baillon and Bleichrodt (2015) used a method similarly tractable as ours. They,
 12 however, used different indexes¹², and they did not establish a control for likelihood.
 13 Several papers used indexes similar to those presented above but provided no controls
 14 for likelihoods, so that they had to use probability intervals or Ellsberg urns (Baillon,
 15 Cabantous, and Wakker 2012; Dimmock, Kouwenberg, and Wakker 2016; Dimmock
 16 et al. 2015, 2016). Li (2017), a follow-up of this paper, used our method to study
 17 linguistic ambiguities. Such ambiguities are among the most common natural ones.
 18 Her sample of Chinese adolescents had an exceptional spread in wealth, allowing for
 19 a good measurement of wealth dependence of ambiguity attitudes. Li, Turmunk, and
 20 Wakker (2017) used our method to measure the impact of ambiguity attitudes in
 21 strategic situations.

22 This paper has shown that the ambiguity aversion index can better be related to
 23 matching probabilities than to nonadditive weighting functions W as done before
 24 (Dow and Werlang 1992; Schmeidler 1989), so as to avoid distortions by risk
 25 attitudes. An additional advantage of matching probabilities is that they are readily
 26 observable. More precisely, we need six indifferences (matching probabilities) to
 27 calculate our two indexes. Measuring a nonadditive function W (a theoretical
 28 construct: Cozic and Hill 2015) is harder, involving other theoretical constructs (U)
 29 and theoretical assumptions. Thus, Abdellaoui et al. (2011) carried out complex
 30 measurements, also involving utilities and beliefs, to obtain their indexes. In this

¹² They used five event-dependent indexes similar to Kilka and Weber (2001), and based on preference conditions of Tversky and Wakker (1995), adapting them to matching probabilities.

1 sense, we make preceding indexes operational (point (d) in intro). Because of point
 2 (f) in the introduction (validity also if EU is violated), our method also works for the
 3 general Choquet expected utility model in Gilboa (1987) which, unlike Schmeidler
 4 (1989), does not assume expected utility for risk; see Baillon, Li, and Wakker (2017).
 5 Key is that risk attitudes, including their deviations, cancel out if we use matching
 6 probabilities.

7 Many studies used introspective likelihood measurements (de Lara Resende and
 8 Wu 2010; Fox, Rogers, and Tversky 1996; Fox and Tversky 1998; Ivanov 2011) to
 9 capture beliefs for natural events. Professional forecasts and survey data are useful
 10 for establishing such beliefs (Anderson, Ghysels, and Juergens 2009). But those are
 11 not revealed preference based and the beliefs may be nonadditive. Then ambiguity
 12 attitudes may be captured partially by those nonadditive stated beliefs and partially by
 13 their weighting functions and, thus, ambiguity attitudes cannot be clearly isolated.
 14 Our paper focuses on clearly defined revealed-preference concepts.

15 In the popular α -maxmin model (Ghirardato, Maccheroni, and Marinacci 2004),
 16 α is often taken as an index of ambiguity aversion. Baillon, Li, and Wakker (2017)
 17 show that, for a popular subclass (priors $(1 - \varepsilon)Q + \varepsilon T$ with Q a fixed focal
 18 probability measure and T variable and any possible probability measure) α can be
 19 recovered from our indexes (where our a is their ε):

$$20 \quad \alpha = \frac{b}{2a} + \frac{1}{2}. \quad (5.1)$$

21 Our b can be taken as an index of absolute ambiguity aversion, and α as a relative
 22 one, being aversion per perceived unit of ambiguity, renormalized. For readers who
 23 prefer the relative index α , our method has also shown how to elicit this for natural
 24 events with unknown subjective beliefs.

25 How ambiguity attitudes are related across different sources of uncertainty, and
 26 across different persons, is an important topic for future research. The isolation of
 27 ambiguity attitudes from likelihood beliefs provided by this paper will be useful for
 28 such research.

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6. CONCLUSION

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Measuring ambiguity attitudes directly from revealed preferences up to now was only possible for artificially created uncertainties because no way was known to correct for unknown likelihood beliefs. We introduce a way to control for such beliefs and, thus, we can define two indexes of ambiguity attitudes that do apply to natural uncertainties as relevant in applications. This increases external validity. Our indexes are valid for many ambiguity theories, unifying and generalizing several existing indexes. In particular, our indexes are valid if expected utility for risk is violated, which is desirable for empirical purposes. Our second index (insensitivity) is needed to capture the likelihood dependence of ambiguity aversion that is usually found empirically.

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We apply our indexes in a study on ambiguity under time pressure. Our findings are psychologically plausible, supporting the validity of our indexes: time pressure affects cognitive components (sensitivity/understanding, or level of ambiguity) but not motivational components (ambiguity aversion). Correlations between successive measurements of our indexes are high, confirming the reliability of our method.

1 APPENDIX A. DETAILS OF THE EXPERIMENT

2 *Procedure*

3 In the experiment, computers of different subjects were separated by wooden panels
4 to minimize interaction between subjects. Brief instructions were read aloud, and
5 tickets with ID numbers were handed out. Subjects typed in their ID numbers to start
6 the experiment. The subjects were randomly allocated to treatment groups through
7 their ID numbers. Talking was not allowed during the experiment. Instructions were
8 given with detailed information about the payment process, user interface, and the
9 type of questions subject would face. The subjects could ask questions to the
10 experimenters at any time. In each session, all subjects started the experiment at the
11 same time.

12 In the TP treatment, we took two measures to make sure that TP would not have
13 any effects in Parts 0 and 2. First, we imposed a two-minute break after Parts 0 and 1,
14 to avoid spill-over of stress from Part 1 to Part 2. Second, we did not tell the subjects
15 that they will be put under TP prior to Part 1, so as to avoid stress generated by such
16 an announcement in Part 0 (Ordonez and Benson 1997).

17

18 *Stimuli: Choice lists*

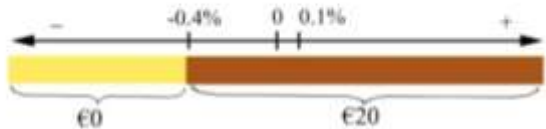
19 Subjects were asked to state which one of the two choice options in §2 they
20 preferred for different values of p , ascending from 0 to 100 (Figures A.1 and A.2).
21 The midpoint between the two values of p where they switched preference was taken
22 as their indifference point and, hence, as the matching probability.

23 To help subjects answer the questions quickly, which was crucial under TP, the
24 experimental webpage allowed them to state their preferences with a single click. For
25 example, if they clicked on Option 2 when the probability of winning was 50%, then
26 for all $p > 50\%$, the option boxes for Option 2 were automatically filled out and for all
27 $p < 50\%$ the option boxes for Option 1 were automatically filled out. This procedure
28 also precluded violations of stochastic dominance by preventing multiple preference
29 switches. After clicking on their choices, subjects clicked on a “Submit” button to
30 move to the next question. The response times were also tracked.

31 In Part 1 of the TP treatment, a timer was displayed showing the time left to
32 answer. If subjects failed to submit their choices before the time limit expired, their

- 1 **Figure A.2: Screenshot of the experiment software for composite event E_{23} in**
- 2 **Part 0**

Which option do you prefer?

Option 1			Option 2
<p>You win €20 if the AEX either decreases by less than 0.4% or increases (and nothing otherwise)</p> 	1	2	<p>You win €20 with the following probability (and nothing otherwise)</p>
	<input checked="" type="radio"/>	<input type="radio"/>	0%
	<input checked="" type="radio"/>	<input type="radio"/>	20%
	<input checked="" type="radio"/>	<input type="radio"/>	35%
	<input checked="" type="radio"/>	<input type="radio"/>	40%
	<input checked="" type="radio"/>	<input type="radio"/>	45%
	<input checked="" type="radio"/>	<input type="radio"/>	50%
	<input checked="" type="radio"/>	<input type="radio"/>	55%
	<input checked="" type="radio"/>	<input type="radio"/>	60%
	<input checked="" type="radio"/>	<input type="radio"/>	65%
	<input checked="" type="radio"/>	<input type="radio"/>	70%
	<input type="radio"/>	<input checked="" type="radio"/>	75%
	<input type="radio"/>	<input checked="" type="radio"/>	80%
	<input type="radio"/>	<input checked="" type="radio"/>	85%
	<input type="radio"/>	<input checked="" type="radio"/>	90%
	<input type="radio"/>	<input checked="" type="radio"/>	93%
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	<input type="radio"/>	<input checked="" type="radio"/>	98%
	<input type="radio"/>	<input checked="" type="radio"/>	99%
	<input type="radio"/>	<input checked="" type="radio"/>	100%

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5 *Stimuli: Avoiding middle bias*

6 The middle bias can distort choice lists: subjects tend to choose the options, in our
 7 case the preference switch, that are located in the middle of the provided range (Erev
 8 and Ert 2013; Poulton 1989). TP can be expected to reinforce this bias. Had we used
 9 a common equally-spaced choice list with, say, 5% incremental steps, then the middle
 10 bias would have moved matching probabilities in the direction of 50% (both for the
 11 single and composite events). This bias would have enhanced the main phenomenon
 12 found in this paper, a-insensitivity, and render our findings less convincing. To avoid
 13 this problem, we designed choice lists that are not equally spaced. In our design, the
 14 middle bias enhances matching probabilities 1/3 for single events and probabilities 2/3
 15 for composite events. Thus, this bias enhances additivity of the matching
 16 probabilities, decreases a-insensitivity, and moves our a-insensitivity index toward 0.
 17 It makes findings of nonadditivity and a-insensitivity more convincing.

1 Table A.1 lists the AEX events that we used. Some questions were repeated for
 2 consistency checks. The corresponding events are listed twice.

3

4 TABLE A.1: List of events on which the AEX prospects were based

Part	Event	Event description
0 (Training)	E ₁	the AEX decreases by strictly more than 0.4%
	E ₁	the AEX decreases by strictly more than 0.4%
	E ₂	the AEX either decreases by less than 0.4% or increases by less than 0.1%
	E ₃	the AEX increases by strictly more than 0.1%
	E ₁₂	the AEX either increases by less than 0.1% or decreases
	E ₂₃	the AEX either decreases by less than 0.4% or increases
	E ₂₃	the AEX either decreases by less than 0.4% or increases
	E ₁₃	the AEX either decreases by strictly more than 0.4% or increases by strictly more than 0.1%
1	E ₁	the AEX decreases by strictly more than 0.2%
	E ₂	the AEX either decreases by less than 0.2% or increases by less than 0.2%
	E ₂	the AEX either decreases by less than 0.2% or increases by less than 0.2%
	E ₃	the AEX increases by strictly more than 0.2%
	E ₁₂	the AEX either increases by less than 0.2% or decreases
	E ₁₂	the AEX either increases by less than 0.2% or decreases
	E ₂₃	the AEX either decreases by less than 0.2% or increases
	E ₁₃	the AEX either decreases by strictly more than 0.2% or increases by strictly more than 0.2%
2	E ₁	the AEX decreases by strictly more than 0.1%
	E ₂	the AEX either decreases by less than 0.1% or increases by less than 0.3%
	E ₃	the AEX increases by strictly more than 0.3%
	E ₃	the AEX increases by strictly more than 0.3%
	E ₁₂	the AEX either increases by less than 0.3% or decreases
	E ₂₃	the AEX either decreases by less than 0.1% or increases
	E ₁₃	the AEX either decreases by strictly more than 0.1% or increases by strictly more than 0.3%
	E ₁₃	the AEX either decreases by strictly more than 0.1% or increases by strictly more than 0.3%

5

6

7 *Incentives*

8 For each subject, one question (i.e., one row of one choice list) was randomly selected
 9 to be played for real at the end of the experiment. If subjects preferred the bet on the
 10 stock market index, then the outcome was paid according to the change in the stock
 11 market index during the duration of the experiment. Bets on the given probabilities

1 were settled using dice. In the instructions of the experiment, subjects were presented
 2 with two examples to familiarize them with the payment scheme. If the time deadline
 3 for a TP question had not been met, the worst outcome (no payoff) resulted.
 4 Therefore, it was in the subjects' interest to submit their choices on time.

5

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9

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